NAME ______________________ **INDEX NUMBER** ____________

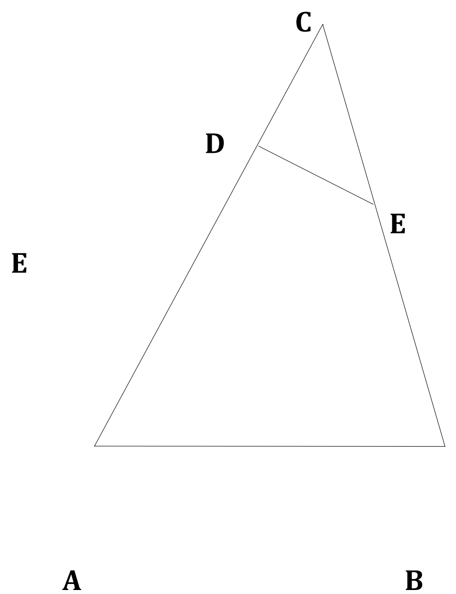
SCHOOL______________________ **DATE**______________________

VECTORS

KCSE 1989 – 2012 Form 3 Mathematics Working Space

1. **1989 Q11 P2**

In the figure below, **AB** = **P**, **AD** = $^{3}/_{5}$ **AC** and **CE** = $^{2}/_{3}$ **CB**



Express **DE** in terms of **p** and **q**

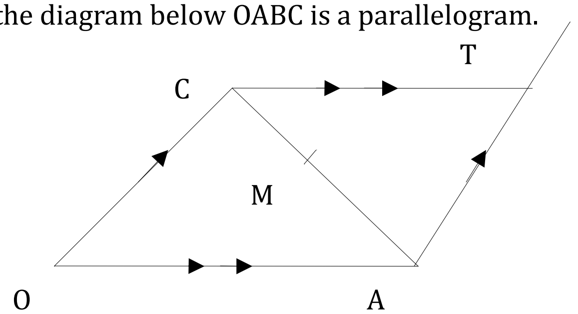
2. **1990 Q21 P1**

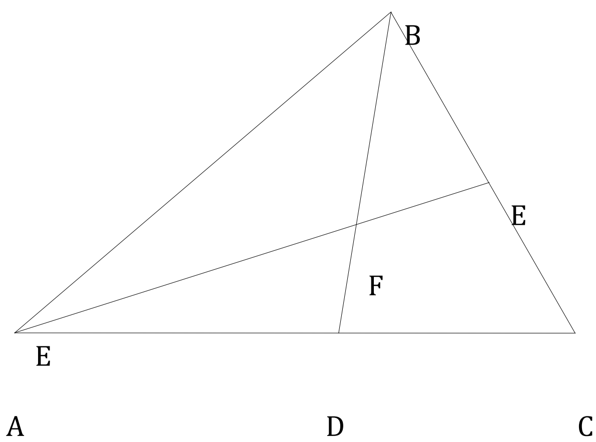
In a parallelogram ABCD, **AB** = 2**a** and **AD** = **b**. M is the midpoint of AB. AC cut MD at X.

i) Express AC in terms of **a** and **b** (2 marks)

ii) Given that **AX** = m**AC** and **MX** = n**MD**, where m and n are constants, find m and n.

(6 marks)

		Working Space
3.	**1990 Q8 P2** In a triangle ABC, D is the midpoint of AB and E is appoint on BC such that BE = $^2/_3$ BC. If **AD** =**P** and **AC** = **Q**, express **EC** in terms of **p** and **q**. (2 marks)	
4.	**1990 Q10 P2** A point T divides a line AB internally in the ratio 5 : 2. Given that A is (-4, 10) And B is (10, 3) find the coordinates of T. (4 marks)	
5.	**1991 Q6 P1** In the diagram below OABC is a parallelogram.  AB is produced to T such that BT: AB = 1:2. M is the midpoint of AC. Given that **OA = a** and **OC = c**. Express MT in term of a and c. (3 marks)	

		Working Space
6.	**1991 Q20 P1** In the figure below E is the midpoint of BC, AD: DC = 3:2 and F is the point of intersection of BD and DE.  i) Given that **AB = b** and **AC = c** express **AE** and **BD** in terms of b and c (3 marks) ii) Given further that **BF** = t**BD** and **AF** = s**AE** find the values of s and t. (5 marks)	
7.	**1992 Q11 P1** Three points A, B and P are in straight line such that **AP** = t**AB**. Given that the coordinates of A, B and P are (3,4) (8,7) and (x,y) respectively, express x and y in term s of t. (3 marks)	

		Working Space
8.	**1992 Q24 P1** OABC is a trapezium such that the coordinates of O,A,B and C ARE (0,0),(2,-1), (4, 3) and (0, y). a) Find the value of y (2 marks) b) M is a midpoint of AB and N is a midpoint of OM. Show that A, N and C are collinear. (6 marks)	
9.	**1992 Q7 P2** The vectors **p, q** and y are expressed in terms of the vectors t and s as follow: **p** = 3**t** + 2s **q** = 5**t** – s **y** = h**t** + (h – k)s where h and k are constants. Given that y = 2**p** – 3**q**, find	

the values of and k. (4 marks)

Working Space

10 **1993 Q21 P1**

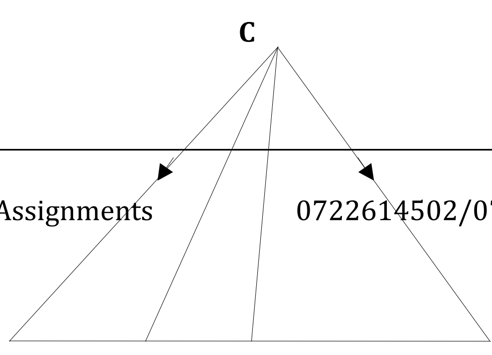
OABC is a trapezium in which **OA = a**, **OC = c** and **CB = 3a**. CB is produced to such that CB : BD = 3: 1. E is a point on AB such that **AB = 2AE**. Show that O, E and d are collinear.

(8 marks)

11 **1993 Q16 P1**

In the figure below **CA** = b **CB** = a, **AX** = **XY** and

AY = **YB**.



b

a

A **X** **Y** **B**

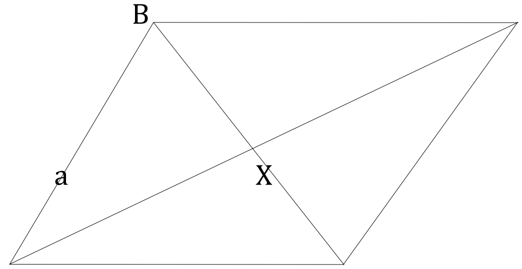
Express CX in terms of a and b (3 marks)

Working Space

12 **1994 Q24 P1**

In the figure below AB = a, AD = b, AX : XC = 2:3 and XB = 4:5

C



A b D

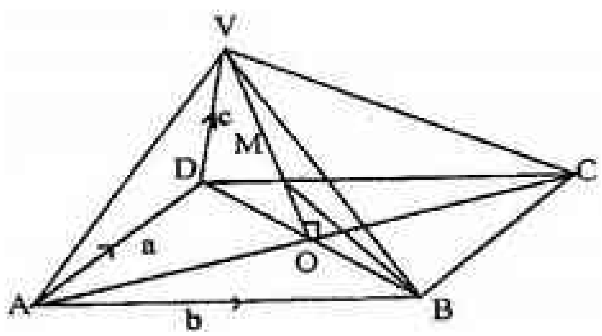
a) Express

i) AC

ii) **DC** in terms of **a** and **b** in the simplest form. (6 marks)

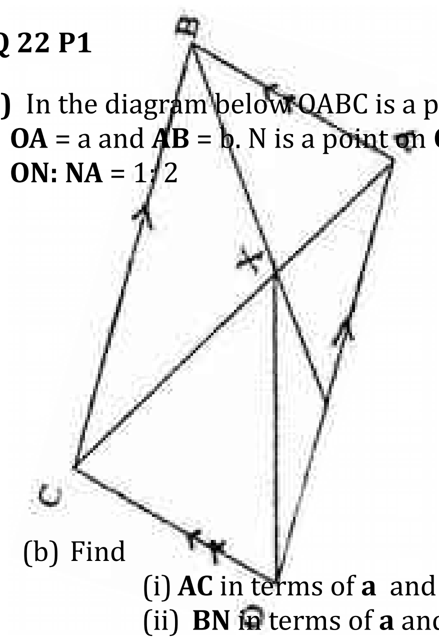
b) If **DC** = n**a** + m**b**, find the values of n and m (2 marks)

13	**1994Q12P2** Find the position vector of point R which divides line MN internally in the ratio 2 : 3. Take the position vectors of M and N to be $\begin{matrix}3\\4\\-6\end{matrix}$ **M** = $\begin{pmatrix}3\\4\\-6\end{pmatrix}$ and **N** = $\begin{pmatrix}-5\\-1\\2\end{pmatrix}$ (3 marks)	Working Space
14	**1994 Q10 P2** In the figure below OC = 3 CA and OD = 3DB. By taking OA = a, OB = b, show that CD // AB. (3 marks) O C D D A B B	
15 .	**1994 Q15 P2** In the figure below ABCD is a parallelogram. AOC and BOD are diagonals of the parallelogram. Show that the diagonals of the parallelogram bisect each other. Give	

	reasons. (3 marks) A B D C	Working Space
16	**1995 Q 18 P1** The figure below is a right pyramid with a rectangular base ABCD and VO as the height. The vectors **AD**= a, **AB** = b and **DV** = c  a) Express (i) **AV** in terms of **a** and **c** (1 mark) (ii) **BV** in terms of **a**, **b** and **c** (2 marks) (b) M is point on **OV** such that **OM: MV** = 3:4, Express **BM** in terms of **a, b** and **c** . Simplify your answer as far as possible (5 marks)	

17 **1996 Q 22 P1**

a) In the diagram below OABC is a parallelogram, **OA** = a and **AB** = b. N is a point on **OA** such that **ON: NA** = 1: 2



(b) Find

(i) **AC** in terms of **a** and **b**

(ii) **BN** in terms of **a** and **b**

(c) The lines AC and BN intersect at X, **AX** = h**AC** and **BX** = k**BN**

(i) By expressing **OX** in two ways, find the values of h and k

(ii) Express **OX** in terms of **a** and **b**

(1 mark)

Working Space

18 **1997 Q 11 P2**

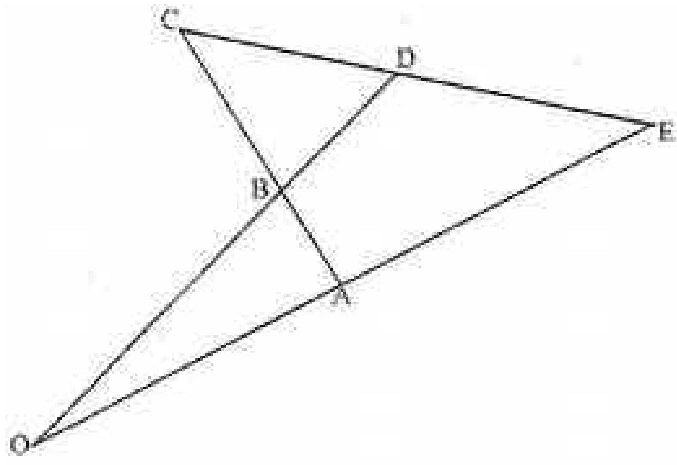
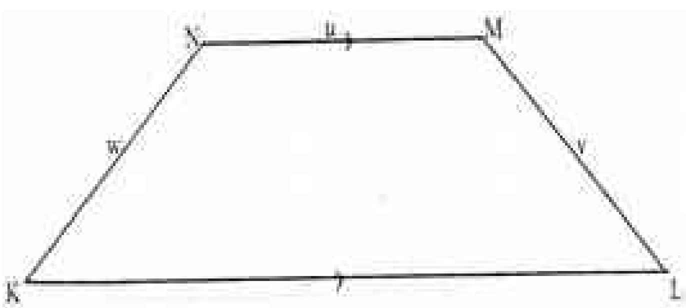
ABC is a triangle and P is on AB such that P divides AB internally in the ratio 4:3. Q is a point on AC such that PQ is parallel to BC. If AC = 14 cm

(i) State the ratio AQ:QC

(ii) Calculate the length of QC

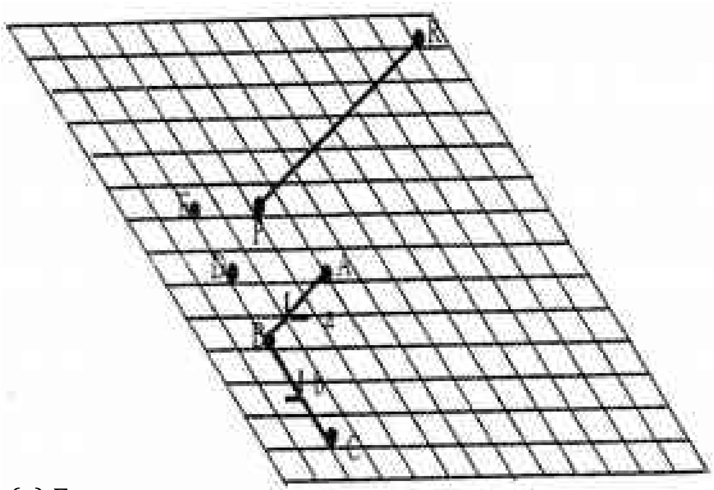
19 **1997 Q 22 P1**

In the figure below **OA** = a, **OB** = b, **AB** = **BC** and **OB: BD** = 3:1

	 (a) Determine **(i) AB** (ii) **CD**, in terms of a and b (b) If CD : DE = 1:k and OA:AE = 1: m determine (i) DE in terms of **a, b** and k	Working Space
20	**1998 Q 9 P2** In the figure, KLMN is a trapezium in which KL is parallel to NM and **KL** = 3 **NM**  Given that **KN** = w, **NM** = u and **ML** = v. Show that 2 u = v= w	
21	**1998 Q 22 P1** The figure below shows a grid of equally spaced	

parallel lines

AB = **a** and BC = **b**



(a) Express

(i) AC in terms of a and b

(ii) AD in terms of a and b.

(b) Using triangle BEP, express BP in terms of a and b

(c) PR produced meets BA produced at X and PR = $^{1}/_{9}\mathbf{b} - {}^{8}/_{3}\mathbf{a}$

By writing PX as kPR and BX as hBA and using the triangle BPX determine the ratio PR: RX

Working Space

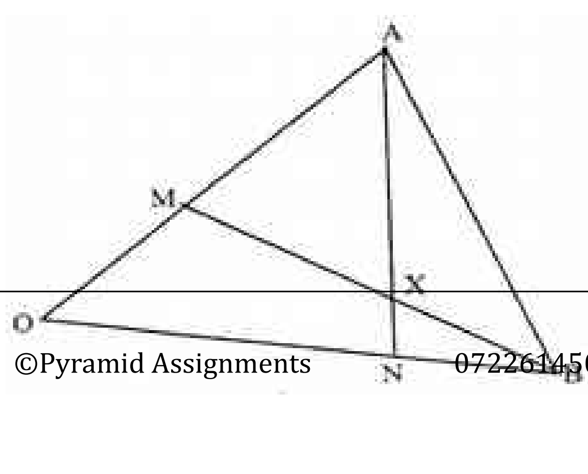
22 **1999 Q 14 P2**

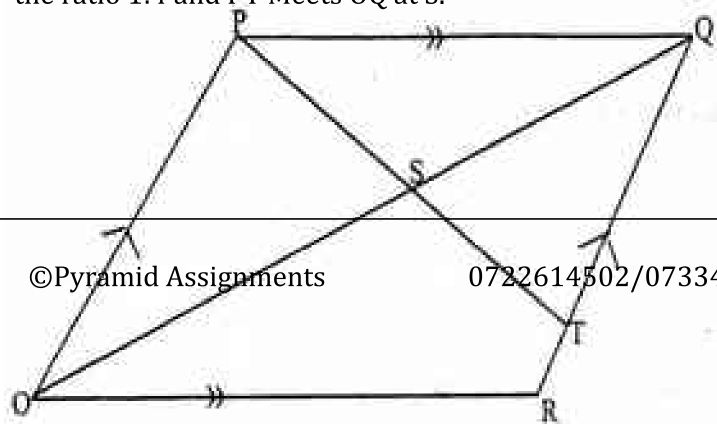
The points P. Q and R lie on a straight line. The position vectors of P and R are 2i + 2j + 13k and 5i – 3j + 4k respectively. Q divides PR Internally in the ratio 2:1.

Find the

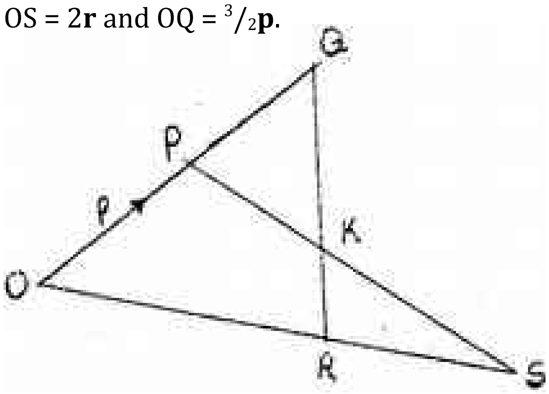
(a) Position vector of Q.

(b) Distance of Q from the origin

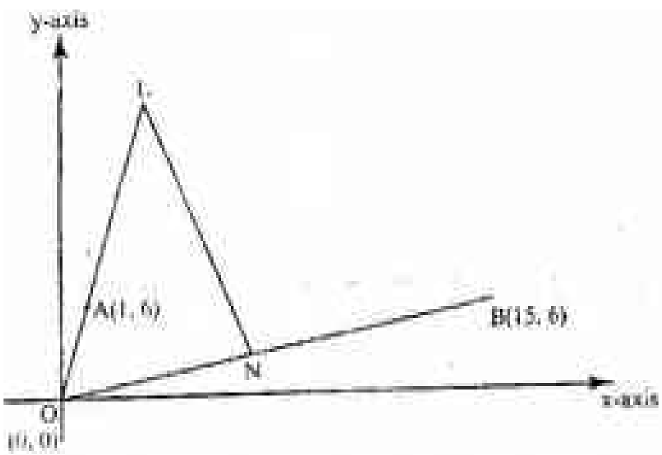
23	**1999 Q 21 P1** In triangle OAB, **OA** = **a, OB** = **b** and P lies on AB such that AP: BP = 3:5 (a) Find the terms of **a** and **b** the vectors **(i)** **AB** **(ii)** **AP** **(iii)** **BP** **(iv)** **OP** (b) Point Q is on OP such AQ = $\frac{-5}{8}$ **a** + $\frac{9}{40}$ _**b.** Find the ratio OQ: QP	Working Space
24	**2000 Q 21 P1** The figure below shows triangle OAB in which M divides OA in the ratio 2: 3 and N divides OB in the ratio 4:1 AN and BM intersect at X.  	

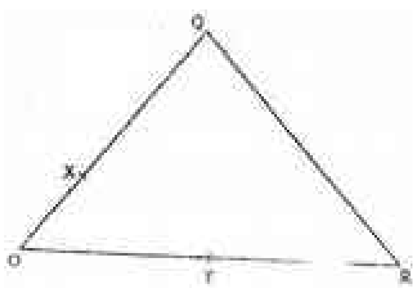
	(a) Given that OA = **a** and OB = **b**, express in terms of a and b: (i) **AN** (ii) **BM** (b)If **AX** = s **AN** and **BX** = t**BM**, where s and t are constants, write two expressions for **OX** in terms of **a,b** s and t. Find the value of s Hence write **OX** in terms of a and b	
25	**2001 Q 16 P1** The position vectors for points P and Q are 4 **i** + 3 **j** + 2**k** and 3**i** – 6**j** + 6**k** respectively. Express vector **PQ** in terms of unit vectors I, j and k. Hence find the length of **PQ**, leaving your answer in simplified form.	Working Space
26	**2001 Q 19 P1** The figure below shows a parallelogram OPQR with O as the origin, **OP** = **p** and **OR = r**, Point T divides RQ in the ratio 1:4 and PT Meets OQ at S. 	

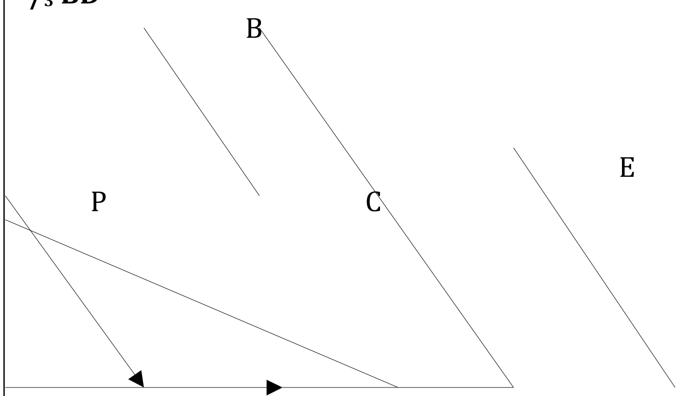
	(a) Express in terms of p and r the vectors (i) **OQ** (ii) **OT** (b) Vector **OS** can be expressed in two ways: m**OQ** or **OT** + n **TP**, Where m and n are constants express **OS** in terms of (i) m, **p** and **r** (ii) n, **p** and **r** Hence find the: (iii) Value on m (iv) Ratio OS: SQ	
27	**2002 Q 10 P2** The coordinates of points O,P,Q and R are (0,0) , (3,4) , (11,6) and (8,2) respectively. A point T is such that vectors **OT,QP** and **QR** satisfy the vector equation. **OT** = **QP** + ½ **QR** .Find the coordinates of T.	Working Space
28	**2002 Q 4 P1** The position vectors of points X and Y are x=2**i** + **j** – 3**k** and y =3i + 2j -2k respectively. Find **XY**	

29	**2003 Q 6 P1** Given that x = 2**i** +**j** – 2**k**,y = - 3**i** +4**j** –**k** and z = - 5**i** +3**j** +2**k** and that p = 3**x** – **y** +2**z**. Find the magnitude of vector p to 3 significant figure (4 marks)	
30	**2003 Q 21 P1** In the figure below, vector OP = **p** and OR =**r**. Vector OS = 2**r** and OQ = $^{3}/_{2}$**p**.  a) Express in terms of p and r (i) **QR** and (ii) **PS** b) The lines QR and PS intersect at K such that **QK** = m **QR** and **PK** = n **PS**, where m and n are scalars. Find two distinct expressions for **OK** in terms of p,r,m and n. Hence find the values of m and n. (5 marks) c) State the ratio PK:KS	Working Space
31	**2004 Q 4 P1** Given that **OA** = 3**i** -2**j** + and **OB** = 4**i** + **j** – 3**k**. Find the	

	distance between points A and B to 2 decimal places.	
32	**2004 Q 21 P1** a) If A, B and C are the points P and Q are p and q respectively is another point with position vector r = $^{3}/_{2}$**q** -$^{1}/_{2}$ **p**. Express in terms of p and q. i) **PR** ii) **RQ** hence shows that P, Q and R are collinear. iii) Determine the ratio PQ: QR.	
33	**2005 Q 13 P1** Point T is the midpoint of a straight line AB. Given the position vectors of A and T are i-j + k and 2i+ 1 ½ k respectively, find the position vector of B in terms of i, j and k. (3 marks)	
34	**2005 Q 18 P1** The points P, Q, R and S have position vectors 2**p**, 3**p**, **r** and 3**r** respectively, relative to an origin O. A point T divides PS internally in the ratio 1:6 (a) Find, in the simplest form, the vectors **OT** and **QT** in terms **P** and **r** (4 marks) (b) (i) Show that the points Q, T, and R lie on a straight line (3 marks) (ii) Determine the ratio in which T divides QR (1 mark)	Working Space

35	**2006 Q 12 P1** Two points P and Q have coordinates (-2, 3) and (1,3) respectively. A translation map point P to P' (10, 10) a) Find the coordinates of Q' the image of Q under the translation (1 mark) (ii) The position vector of **P** and **Q** in (a) above are p and q respectively given that $m\mathbf{p} - n\mathbf{q} = \begin{pmatrix} -12 \\ 9 \end{pmatrix}$ (3 marks) b) Find the value of *m* and *n*	
36	**2006 Q 22 P1** In the diagram below, the coordinates of points A and B are (1, 6) and (15, 6) respectively. Point N is on OB such that 3 ON = 2OB. Line OA is produced to L such that OL = 3 OA  (a) Find vector LN (3 marks) (b) Given that a point M is on LN such that LM: MN = 3: 4, find the coordinates of (2 marks) (c) If line OM is produced to T such that OM: MT = 6:1 (i) Find the position vector of T (1 mark) (ii) Show that points L, T and B are collinear (4 marks)	Working Space

37	**2006 Q 9 P2** Given that q **i** + $^{1}/_{3}$ **j** + $^{2}/_{3}$ **k** is a unit vector, find q (2 marks)	
38	**2007 Q 21 P1** In the figure below, **OQ** = q and **OR** = r. Point X divides OQ in the ratio 1: 2 and Y divides OR in the ratio 3: 4 lines XR and YQ intersect at E.  (a)Express in terms of q and r (i) **XR** (1 mark) (ii) **YQ** (1 mark) (b) If **XE** = m **XR** and **YE** = n **YQ**, express **OE** in terms of: (1 mark) (i) r, q and m (ii) r, q and n (1 mark) (c) Using the results in (b) above, find the values of m and n. (6 marks)	

		Working Space
39	**2007 Q 12 P2** Vector q has a magnitude of 7 and is parallel to vector p. Given that p= 3 **i** –**j** + 1 ½ **k**, express vector q in terms of i, j, and k. (2 marks)	
40	**2008 Q 19 P2** In the figure below **AB=p, AD= q, DE= ½ AB and BC= $^{2}/_{3}$ BD**  A D a) Find in terms of p arid q the vectors: (1 mark) (i) **BD**; (1 mark) (ii) **BC**; (1 mark) (iii) **CD**; (1 mark) (iv) **AC**. (2 marks) b) Given that **AC**=*k***CE**, where *k* is a scalar, find (i) The value of *k* (4 marks) (ii) The ratio in which C divides AE (1 mark)	

		Working Space
41	**2008 Q 4 P2** The position vectors of points A and B are $\begin{pmatrix} 3 \\ -1 \\ -4 \end{pmatrix}$ and $\begin{pmatrix} 8 \\ -6 \\ 6 \end{pmatrix}$ respectively. A point P divides AB in AB it he ratio 2:3. Find the position Vector of point P. (3 marks)	
42	**2009 Q 20 P1** The position vectors of point A and B with respect to the O,are $\begin{pmatrix} -8 \\ 5 \end{pmatrix}$ and $\begin{pmatrix} 12 \\ -5 \end{pmatrix}$ respectively Point M is the midpoint of AB and N is the midpoint of OA. (a) Find: i) The coordinates of N and M (3 marks) ii) The magnitude of NM (3 marks) (b) Express vector **NM** in term of **OB**. (c) Point P maps onto P by a translation $\begin{pmatrix} -5 \\ 8 \end{pmatrix}$ Given that **OP**=**OM**+2**MN**, find the coordinates of P´	

43 **2009 Q 6 P2**

Vector **OA** = $\begin{pmatrix} 2 \\ 1 \end{pmatrix}$ and **OB**= $\begin{pmatrix} 6 \\ -3 \end{pmatrix}$ Point C is on

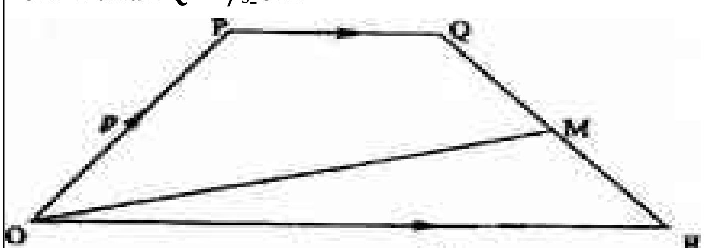
OB such CB=2OC and point D is on AB such that AD=3DB.

Express **CD** as a column vector. (3 marks)

Working Space

44 **2010 Q 7 P1**

In the figure below, OPQR is a trapezium in which PQ is parallel to OR and M is the mid-point of QR and **OP=p, OR=r** and **PQ** = $^1/_3$ **OR**.



Find **OM** in terms of **p** and **r.** (3 marks)

45 **2010 Q 18 P2**

In the figure below OJKL is a parallelogram in which OJ = 3p and OL = 2r

L K

2r

O 3p J

a) If A is a point on LK such that LA = ½ AK and point B divide the line JK externally in the ratio 3:1, express **OB** and **AJ** in terms of **p** and **r.** (2 marks)

b) Line OB interests AJ at X such that **OX** = m**OB** and **AX** = n**AJ.**

   i) Express **OX** in terms of **p, r** and m. (1 mark)

   ii) Express **OX** in terms of **p, r** and n (1 mark)

   iii) Determine the value of *m* and *n* and hence the ratio in which point x divides line AJ. (6 marks)

Working Space

46

2011 Q 13 P2

Vector **OP**=6**i** + **j** and **OQ**+ -2**i** +5**j**. A point N divides **PQ** internally in the ratio 3:1. Find **PN** in terms of i and j. (3 marks)

47

2011 Q 23 P1

In the figure below,ABCD is a trapezium. AB is parallel to DC,diagonals AC and DB intersect at X and DC=2AB. **AB= a, DA=d, AX=**k **AC** and **DX**= h**DB** where h and k are constants.

A a B

d X

D C

a) Find in terms of a and d

i) BC (2 marks)

ii) AX (2 marks)

iii) DX (1 mark)

48 **2012 Q4 P2**

Given that $\boldsymbol{P}=2\boldsymbol{i}-3\boldsymbol{j}+\boldsymbol{k}$, $\boldsymbol{Q}=3\boldsymbol{i}-4\boldsymbol{j}-3\boldsymbol{k}$ and $\boldsymbol{R}=3\boldsymbol{P}+2\boldsymbol{Q}$, find the magnitude of $\boldsymbol{R}$ to 2 significant figures. (3 marks)

Working Space

49 **2012 Q19 P2**

In triangle OPQ below, **OP** = **p**, **OQ**=**q**. Point M lies on **OP** such that **OM**: **MP**=2:3 and point N lies on **OQ** such that **ON**: **NQ**=5:1. Line PN intersects line MQ at X.

P

p

M

O Q

q

(a) Express in terms of **p** and **q**:

(i) **PN;** (1 mark)

ii) **QM;** (1 mark)

(b) Given that **PX**= k**PN** and **QX**=r**QM,**where k and r are scalars:

(i) Write two different expressions for OX in terms of **p**,**q**,k and r; (2 marks)

(ii) Find the values of k and r; (4 marks)

(iii) Determine the ratio in which X divides line MQ. (2 marks)